Chem1B, General Chemistry II

1.) Both $H_2PO_4^-$ ($K_a = 4.2 \times 10^{-13}$) and HSO_3^- ($K_a = 6.2 \times 10^{-8}$) are amphiprotic (amphoteric). Write out the expected equilibrium formed between these compounds, clearly indicating which will behave as the acid and which as the base.

Since HSO₃ has a higher Ka, it is the stronger acid and will donate the proton to H₂PO₄

```
HSO_3^{-1}(aq) + H_2PO_4^{-1}(aq) \leftrightarrow SO_3^{-2}(aq) + H_3PO_4(aq)
```

2.) Consider a buffer solution created by mixing formic acid with formate by the following equilibrium.

```
HCHO_2(aq) + H_2O(1) \leftrightharpoons CHO^{2-}(aq) + H_3O^{+}(aq) K_a = 1.8 \times 10^{-4}
```

a.) Calculate the grams of magnesium formate (Mg(CHO₂)₂, 114.35 g/mol) needed to be dissolved in 1.50 L of 0.25 M formic acid to obtain a pH of 4.23.

```
4.23 = -\log(1.8 \times 10^{-4}) + \log([\text{base}]/0.25 \text{ M})

0.48\underline{5}2 = \log([\text{base}]/0.25)

[base] = 0.76\underline{4}2 M

0.76\underline{4}2 mols/L x (1.50 L) = 1.1\underline{4}6 moles formate

1.1\underline{4}6 mols formate × \frac{1 \text{ mole Mg(CHO}_2)_2}{2 \text{ moles CHO}_2^2} × \frac{114.35 \text{ g Mg(CHO}_2)_2}{1 \text{ mole Mg(CHO}_2)_2} = 65.\underline{5}4 \Rightarrow 65.5 g Mg(CHO<sub>2</sub>)<sub>2</sub>
```

b.) To the buffer solution in (a), 0.125 moles of sodium hydroxide (NaOH) are added without changing the volume of the solution. Calculate the new pH of the buffer.

NaOH is a strong base and will reduce the acid and add to the conjugate base.

```
\frac{0.25 \text{ moles acid}}{1 \text{ L solution}} \times 1.50 \text{ L solution} = 0.375 \text{ moles HCHO}_2 \text{ initially}
0.375 \text{ moles HCHO}_2 \text{ initially} - 0.125 \text{ mols NaOH} = 0.250 \text{ moles HCHO}_2 \text{ in excess}
0.125 \text{ moles NaOH} \times \frac{1 \text{ mole formate}}{1 \text{ mole NaOH}} = 0.125 \text{ moles formate produced}
1.1\underline{4}6 \text{ moles CHO}_2^- \text{ initially} + 0.125 \text{ moles CHO}_2^- \text{ produced} = 1.2\underline{7}1 \text{ moles CHO}_2^-
pH = -\log(1.8 \times 10^{-4}) + \log\left(\frac{\frac{1.271 \text{ moles formate}}{0.250 \text{ moles acid}}}{\frac{1.50 \text{ L solution}}{0.250 \text{ moles acid}}}\right)
pH = -\log(1.8 \times 10^{-4}) + 0.7062 = 4.4509 \rightarrow \textbf{4.451} \text{ (should be higher than (a))}
```

c.) To the buffer solution in (a), 0.135 moles of hydrobromic acid (HBr) are added without changing the volume of the solution. Calculate the new pH of the buffer.

HBr is a strong acid and will reduce the amount of conjugate base and add to the acid.

- $1.1\underline{46}$ moles CHO₂ initially 0.135 moles HBr = $1.0\underline{1}$ 1 moles CHO₂ excess
- 0.135 moles HBr $\times \frac{1 \text{ mole acid produced}}{1 \text{ mole HBr}} = 0.135 \text{ moles acid produced}$
- 0.375 moles HCHO₂ initially + 0.135 moles HBr = 0.51 moles HCHO₂

pH =
$$-\log(1.8 \times 10^{-4}) + \log\left(\frac{\frac{1.011 \text{ moles formate}}{1.50 \text{ L solution}}}{\frac{0.51 \text{ moles acid}}{1.50 \text{ L solution}}}\right)$$

pH = $-\log(1.8 \times 10^{-4}) + 0.29\overline{7}1 = 4.04\underline{1}9 \rightarrow \textbf{4.042}$ (should be lower than (a))

- 3.) Consider the following compounds all at 0.100 M: HNO₃, NaOH, NH₃ ($K_b = 1.8 \times 10^{-5}$), HClO₂ ($K_a = 1.1 \times 10^{-2}$).
 - a.) Arrange the above in order of increasing pH, from lowest to highest.

```
HNO<sub>3</sub>, HClO<sub>2</sub>, NH<sub>3</sub>, NaOH
```

b.) Arrange the above in order of increasing % ionization, from lowest to highest.

$$NH_3$$
, $HClO_2$, $HNO_3 = NaOH$

Chem1B, General Chemistry II

4.) Should a precipitate of Mg(OH)₂(s) form in a solution made from 0.010 M MgCl₂ and 0.10 M NH₃? The K_b for NH₃ is 1.8×10^{-5} , and the K_{sp} for Mg(OH)₂ is 1.8×10^{-11} .

$$\begin{split} [\text{Mg}^{2+}] &= 0.010 \text{ M MgCl}_2 \times \frac{1 \text{ mole Mg}^{2+}}{1 \text{ mole MgCl}_2} = 0.010 \text{ M Mg}^{2+} \\ &\qquad \text{NH}_3(\text{aq}) + \qquad \text{H}_2\text{O}(\text{aq}) \longleftrightarrow \qquad \text{NH}_4^+(\text{aq}) + \qquad \text{OH}^-(\text{aq}) \\ \text{I} &\qquad 0.10 \text{ M} \qquad \qquad 0 \qquad \qquad 0 \\ \text{C} &\qquad -x \qquad \qquad +x \qquad \qquad +x \\ \text{E} &\qquad 0.10-x \qquad \qquad x \qquad \qquad x \\ \text{K}_b &= 1.8 \times 10^{-5} = \frac{[\text{NH}_4^+][\text{OH}^-]}{[\text{NH}_3]} = \frac{x^2}{0.10} \text{ (ignoring -x due to low \% ionization)} \\ x^2 &= 1.8 \times 10^{-6} \longrightarrow x = 1.\underline{3}4 \times 10^{-3} \text{ M} = [\text{OH}^-] \\ \text{Q} &= (0.010 \text{ M})(1.34 \times 10^{-3})^2 = 1.8 \times 10^{-8}, \text{ Q} > \text{K}_{\text{Sp}} \text{ so } \textbf{yes}, \text{ the salt will precipitate.} \end{split}$$

- 5.) Consider the titration of a 30.0 mL portion of 0.20 M HF ($K_a = 6.6 \times 10^{-4}$) with 0.10 M NaOH.
 - a.) Calculate the initial pH of the solution when 0 mL of NaOH has been added.

HF(aq) + H₂O(I)
$$\leftarrow$$
 > H₃O⁺(aq) + F⁻(aq)
0.20 0 0 0
C - x + x + x
E 0.20 - x x x x
 $6.6 \times 10^{-4} = \frac{x^2}{0.20}$ (ignoring -x due to low % ionization)
 $x^2 = 1.\underline{3}2 \times 10^{-4} \rightarrow x = 0.01\underline{1}4 = [H_3O^+]$
pH = - log(0.0114) = 1.9 $\underline{3}9 \rightarrow$ **1.94**

b.) Calculate the pH of the solution after 10.0 mL of NaOH have been added.

```
10.0 mL NaOH × \frac{1 \text{ L}}{1000 \text{ mL}} × \frac{0.10 \text{ mols NaOH}}{1 \text{ L}} × \frac{1 \text{ mol HF}}{1 \text{ mol NaOH}} = 1.0 × 10<sup>-3</sup> moles HF used 30.0 mL HF initial × \frac{1 \text{ L}}{1000 \text{ mL}} × \frac{0.20 \text{ moles HF}}{1 \text{ L}} = 6.0 × 10<sup>-3</sup> moles HF initial 6.0 × 10<sup>-3</sup> initial – 1.0 × 10<sup>-3</sup> used = 5.0 × 10<sup>-3</sup> mols HF in excess moles NaOH added = moles F<sup>-</sup> produced, so moles F<sup>-</sup> = 1.0 × 10<sup>-3</sup> moles [HF] = (5.0 \times 10^{-3} \text{ moles})/(0.030 \text{ L} + 0.010 \text{ L}) = 0.125 M [F<sup>-</sup>] = 1.0 × 10<sup>-3</sup> moles/(0.030 L + 0.010 L) = 0.025 M pH = -log(6.6 × 10<sup>-4</sup>) + log(0.025/0.125) = 2.481 \rightarrow 2.48
```

c.) Calculate the pH of the solution at equivalence point.

 $\begin{array}{l} 6.0\times 10^{\text{-3}} \text{ moles HF initial} = 6.0\times 10^{\text{-3}} \text{ moles NaOH added} = 6.0\times 10^{\text{-3}} \text{ moles F}^{\text{-}} \text{ present} \\ 6.0\times 10^{\text{-3}} \text{ moles NaOH x (1 L/0.10 moles NaOH)} = 0.06 \text{ L added to reach equiv.} \\ \text{[F}^{\text{-}}] = 6.0\times 10^{\text{-3}} \text{ moles/(0.06 L + 0.030 L)} = 0.06\underline{6}6 \text{ M} \\ \text{F}^{\text{-}}(\text{aq}) + \text{H}_2\text{O(I)} \longleftrightarrow \text{HF(aq)} + \text{OH}^{\text{-}}(\text{aq}) \\ \text{I} \qquad 0.066 \qquad 0 \qquad 0 \\ \text{C} \qquad -x \qquad +x \qquad +x \\ \text{E} \qquad 0.066-x \qquad x \qquad x \\ \text{K}_b = (1.0\times 10^{\text{-14}})/(6.6\times 10^{\text{-4}}) = 1.\underline{5}1\times 10^{\text{-11}} = \frac{x^2}{0.066} \text{ (ignoring -x term due to low \% ion)} \\ \text{x}^2 = 1.0\times 10^{\text{-12}} \longrightarrow \text{x} = 1.0\times 10^{\text{-6}} = \text{[OH-] so pOH} = -\text{log}(1.0\times 10^{\text{-6}}) = 6.00 \end{array}$

$$pH = 14 - 6.00 = 8.00$$

Chem1B, General Chemistry II

6.) Calculate the total change in entropy (ΔS_{total}) for 18.3 g of H₂O(s) (18.016 g/mol) at 273 K to melt in a container held at 315 K, given that the heat of fusion (ΔH_{fus}) for water is 6.02 kJ/mol at 0 K. Assume complete heat transfer from the ice to the surrounding air.

```
18.3 \text{ g ice} \times \frac{1 \text{ mole ice}}{18.016 \text{ g ice}} \times \frac{6.02 \text{ kJ}}{1 \text{ mole ice}} = 6.1\underline{1}4 \text{ kJ absorbed by system, lost by surroundings} \Delta S_{\text{sys}} = (6.1\underline{1}4 \text{ kJ})/273 \text{ K} = 0.022\underline{3}9 \text{ kJ/K} \Delta S_{\text{surr}} = (-6.1\underline{1}4 \text{ kJ})/315 \text{ K} = -0.019\underline{4}1 \text{ kJ/K} \Delta S_{\text{total}} = 0.022\underline{3}9 \text{ kJ/K} - 0.019\underline{4}1 \text{ kJ/K} = 2.9\underline{7}7 \times 10^{-3} \text{ kJ/K x } 1000 \text{ J/kJ} \rightarrow \textbf{2.98 J/K}
```

7.) Consider the following equilibrium:

$$AI(OH)_3(s) \leftrightharpoons AI^{3+}(aq) + 3 OH^{-}(aq)$$
 $K_{sp} = 1.3 \times 10^{-33}$

A solution has $[Al^{3+}] = 0.075$ M and $[HC_2H_3O_2] = 1.00$ M. What is the maximum quantity, in g, of $NaC_2H_3O_2$ (82.03 g/mol) that can be added to 250.0 mL of this solution before precipitation of $Al(OH)_3(s)$ begins? K_a for acetic acid is 1.8×10^{-5} .

```
\begin{split} &\mathsf{K}_{\mathsf{sp}} = 1.3 \times 10^{-33} = [\mathsf{AI}^{3+}][\mathsf{OH}^-]^3 = (0.075 \; \mathsf{M})(\mathsf{x})^3 \xrightarrow{} \mathsf{x} = 2.\underline{5}8 \times 10^{-11} = [\mathsf{OH}^-] \\ &\mathsf{pOH} = -\log(2.58 \times 10^{-11}) = 10.5\underline{8}7, \; \mathsf{so} \; \mathsf{pH} = 14 - 10.5\underline{8}7 = 3.4\underline{1}2 \; \mathsf{at} \; \mathsf{saturation} \\ &3.4\underline{1}2 = -\log(1.8 \times 10^{-5}) + \log(\mathsf{x}/1.00) \\ &-1.3\underline{3}1 = \log(\mathsf{x}/1.00) \\ &10^{-1.331} = 0.04\underline{6}5 = \mathsf{x}/1.00 \xrightarrow{} \mathsf{x} = 0.04\underline{6}5 = [\mathsf{C}_2\mathsf{H}_3\mathsf{O}_2^-] \\ &0.04\underline{6}5 \; \mathsf{moles} \; \mathsf{C}_2\mathsf{H}_3\mathsf{O}_2^-/1 \; \mathsf{L} \; \mathsf{x} \; 0.2500 \; \mathsf{L} \; \mathsf{solution} = 0.01\underline{1}6 \; \; \mathsf{moles} \; \mathsf{C}_2\mathsf{H}_3\mathsf{O}_2^- \\ &0.01\underline{1}6 \; \mathsf{moles} \; \mathsf{C}_2\mathsf{H}_3\mathsf{O}_2^- \times \frac{1 \; \mathsf{mole} \; \mathsf{sodium} \; \mathsf{acetate}}{1 \; \mathsf{mole} \; \mathsf{sodium} \; \mathsf{acetate}} \times \frac{82.03 \; \mathsf{g}}{1 \; \mathsf{mole} \; \mathsf{sodium} \; \mathsf{acetate}} = 0.9\underline{5}5 \\ &\longrightarrow \boldsymbol{0.96} \; \boldsymbol{g} \; \boldsymbol{\mathsf{NaC}_2\mathsf{H}_3\mathsf{O}_2} \end{split}
```